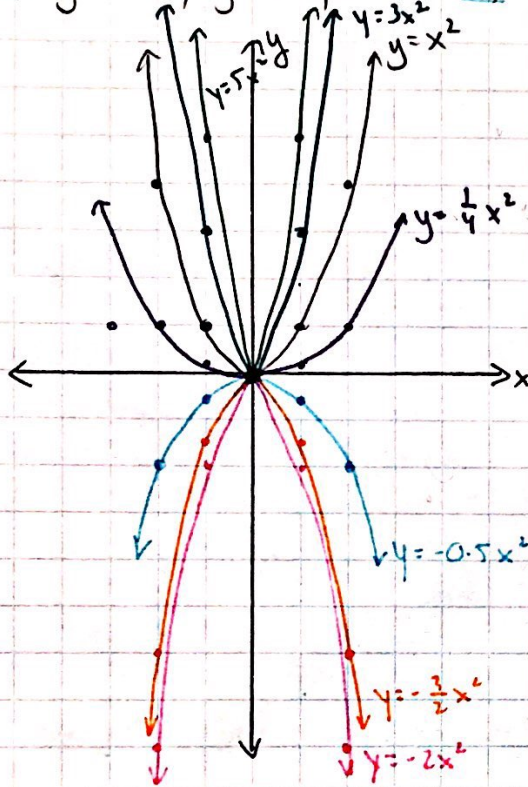


# 5.1 Stretching and Reflecting Quadratic Relations.

- 1a) iv      2a)  $(1, 1)$ ,  $a=5$       b)  $(-2, 4)$ ,  $a=-3$       c)  $(5, 25)$ ,  $a=-0.6$       d)  $(-4, 16)$ ,  $a=\frac{1}{2}$   
 b) iii       $\downarrow$        $\downarrow$        $\downarrow$        $\downarrow$   
 c) i       $(1, 5)$        $(-2, -12)$        $(5, 15)$        $(-4, 8)$   
 d) ii

- 3a)  $y=2x^2$ ,  $y=4x^2$ , etc.      b)  $y=-\frac{1}{3}x^2$ ,  $y=-\frac{1}{2}x^2$ , etc      c)  $y=-4x^2$ ,  $y=-5x^2$ , etc

4.



x	a) $y=x^2$	b) $y=3x^2$	c) $y=-0.5x^2$	d) $y=2x^2$	e) $y=\frac{1}{4}x^2$	f) $y=-\frac{3}{2}x^2$	g) $y=5x^2$
-2	4	12	-2	-8	1	-6	20
-1	1	3	-0.5	-2	1/4	-3/2	5
0	0	0	0	0	0	0	0
1	1	3	-0.5	-2	1/4	-3/2	5
2	4	12	-2	-8	1	-6	20

- 5a) v.s. by a factor of 5,  $y=5x^2$   
 b) v.c. by a factor of  $\frac{1}{2}$ , reflect over x;  $y=-\frac{1}{2}x^2$   
 c) reflect over x-axis, v.s. by a factor of 2.5;  $y=-2.5x^2$   
 d) v.c. by a factor of  $\frac{1}{4}$ ;  $y=\frac{1}{4}x^2$

6. Move over two and down  $\frac{1}{2}$  from the vertex.  
 Usually you would go over 2 and up 4.  
 $4x - \frac{1}{2}$  is  $-\frac{1}{2}$ , so the equation is  $y=-\frac{1}{8}x^2$ .

7a)  $y=ax^2$ , point at  $(3, -3)$   
 $-3 = a(3)^2$   
 $-3 = 9a$   
 $-\frac{1}{3} = a$   
 $y = -\frac{1}{3}x^2$

- 8a) v.s. by a factor of 4.      b) v.c. by a factor of  $\frac{2}{3}$ , v.ref.  
 $(2, 4) \xrightarrow{(x, y)} (2, 16)$        $(2, 4) \xrightarrow{(x, y)} (2, -8/3)$   
 c) v.c. by a factor of 0.25      d) v.reflection, v.s. by a factor of 5  
 $(2, 4) \xrightarrow{(x, y)} (2, 1)$        $(2, 4) \xrightarrow{(x, y)} (2, -20)$   
 e) reflect over the x-axis      f) v.c. by a factor of  $\frac{1}{5}$   
 $(2, 4) \xrightarrow{(x, y)} (2, -4)$        $(2, 4) \xrightarrow{(x, y)} (2, 75)$

b)  $y=ax^2$ , point at  $(-3, -2)$   
 $-2 = a(-3)^2$   
 $-2 = 9a$   
 $-\frac{2}{9} = a$   
 $y = -\frac{2}{9}x^2$

10. a values of 1 or -1 result in the same shape.

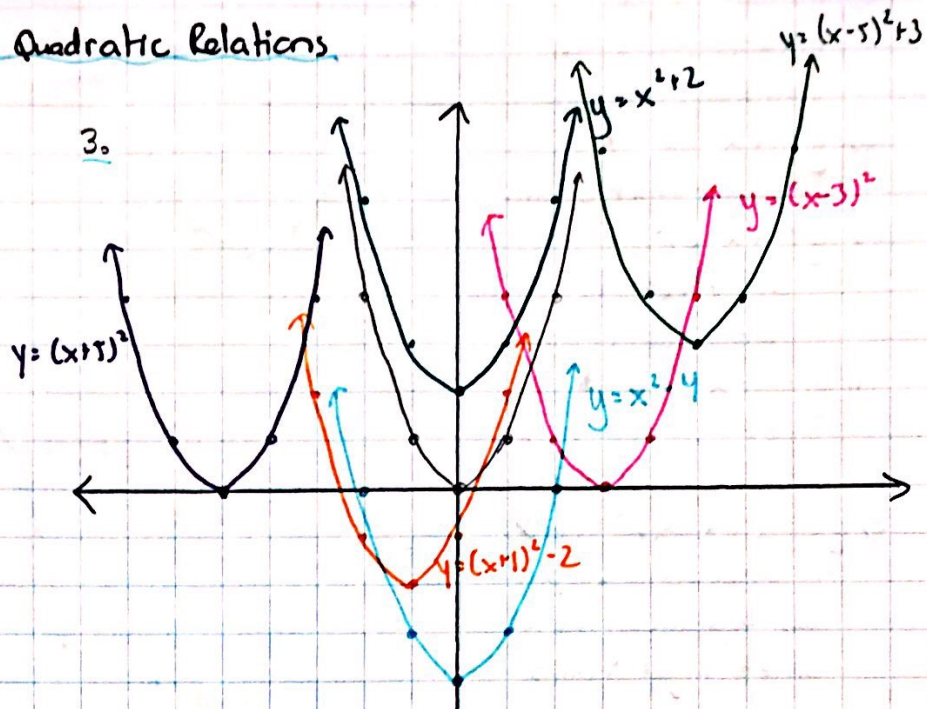
ll. Equation	Opens	Stretch/compress	Wider/Narrower
a) $y=5x^2$	up	stretch	narrow
b) $y=0.25x^2$	up	compress	wide
c) $y=-\frac{1}{3}x^2$	down	compress	wide
d) $y=-8x^2$	down	stretch	narrow.

- 12a)  $a < 0$  means a is  $\ominus$ .  
 b) Multiplying by a fraction makes y smaller  
 c) No shift.

## 5.2 Exploring Translations of Quadratic Relations

- a)  $h=3, k=0$   
 $y = (x-3)^2$   
 b)  $k=-4, h=0$   
 $y = x^2 - 4$   
 c)  $h=-2, k=0$   
 $y = (x+2)^2$   
 d)  $k=5, h=0$   
 $y = x^2 + 5$   
 e)  $k=-7, h=-6$   
 $y = (x+6)^2 - 7$   
 f)  $h=2, k=5$   
 $y = (x-2)^2 + 5$

- 2a) (iii)  
 b) (v)  
 c) (ii)  
 d) (iv)

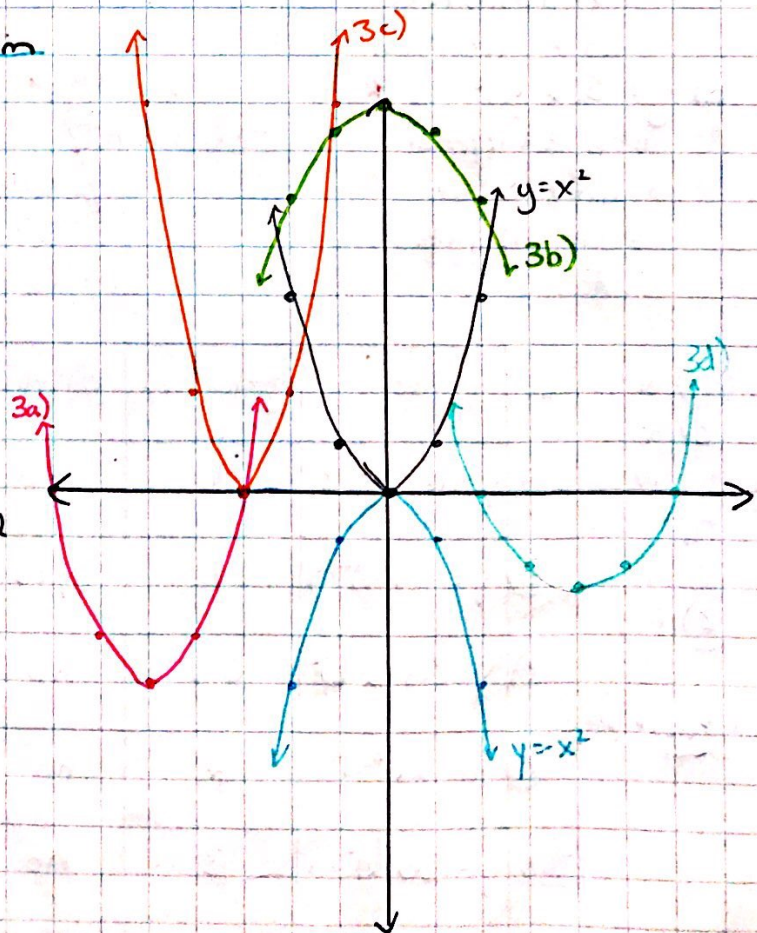


- 4a)  $y = x^2 + 5$   
 • shift up 5 units  
 b)  $y = (x-3)^2$   
 • shift left 3 units  
 c)  $y = -3x^2$   
 • reflect over x-axis  
 • v.c. by a factor of 3  
 d)  $y = (x+7)^2$   
 • shift left 7 units  
 e)  $y = \frac{1}{2}x^2$   
 • v.c. by a factor of  $\frac{1}{2}$   
 f)  $y = (x+6)^2 + 12$   
 • shift left 6 units  
 and up 12 units.

S.	Equation	Vertex	A of S
a)	$y = x^2 + 5$	(0, 5)	$x=0$
b)	$y = (x-3)^2$	(3, 0)	$x=3$
c)	$y = -3x^2$	(0, 0)	$x=0$
d)	$y = (x+7)^2$	(-7, 0)	$x=-7$
e)	$y = \frac{1}{2}x^2$	(0, 0)	$x=0$
f)	$y = (x+6)^2 + 12$	(-6, 12)	$x=-6$

## 5.3 Graphing Quadratics in Vertex Form

- 1a)  $y = x^2 - 3$   
 • shift down 3 units  
 b)  $y = (x+5)^2$   
 • shift left 5 units  
 c)  $y = -\frac{1}{2}x^2$   
 • reflect over x-axis  
 • v.c. by a factor of  $\frac{1}{2}$   
 d)  $y = 4(x+2)^2 - 16$   
 • v.s. by a factor of 4  
 • shift left 2 units  
 and down 16 units  
 2a) opens up,  
 (0, -3),  $x=0$   
 b) opens up,  
 (-5, 0),  $x=-5$   
 c) opens down  
 (0, 0),  $x=0$   
 d) opens up  
 (-2, -16),  $x=-2$



3.

x	$y = x^2$	$y = -x^2$	$y = \frac{1}{2}x^2$	$y = 2x^2$
-2	4	-4	-2	8
-1	1	-1	$-\frac{1}{2}$	2
0	0	0	0	0
1	1	-1	$\frac{1}{2}$	2
2	4	-4	2	8

- 4a)  $y = -x^2 + 9$  \*
- reflect over x-axis
  - shift up 9 units
- b)  $y = (x-3)^2$  \*
- shift right 3 units
- c)  $y = (x+2)^2 - 1$  \*
- shift left two units and down 1 unit.
- d)  $y = -x^2 - 6$  \*
- reflect over x-axis
  - shift down 6 units
- e)  $y = -2(x-4)^2 + 16$  \*
- reflect over x-axis
  - v.s. by a factor of 2
  - shift right 4 units and up 16 units
- f)  $y = \frac{1}{2}(x+6)^2 + 12$  \*
- v.c. by a factor of  $\frac{1}{2}$
  - shift left 6 units up 12 units.
- g)  $y = -\frac{1}{2}(x+4)^2 - 7$  \*
- reflect over x-axis
  - v.c. by a factor of  $\frac{1}{2}$
  - shift 4 units left and 7 units down
- h)  $y = 5(x-4)^2 - 12$  \*
- v.s. by a factor of 5
  - shift 4 units right + 12 units down.

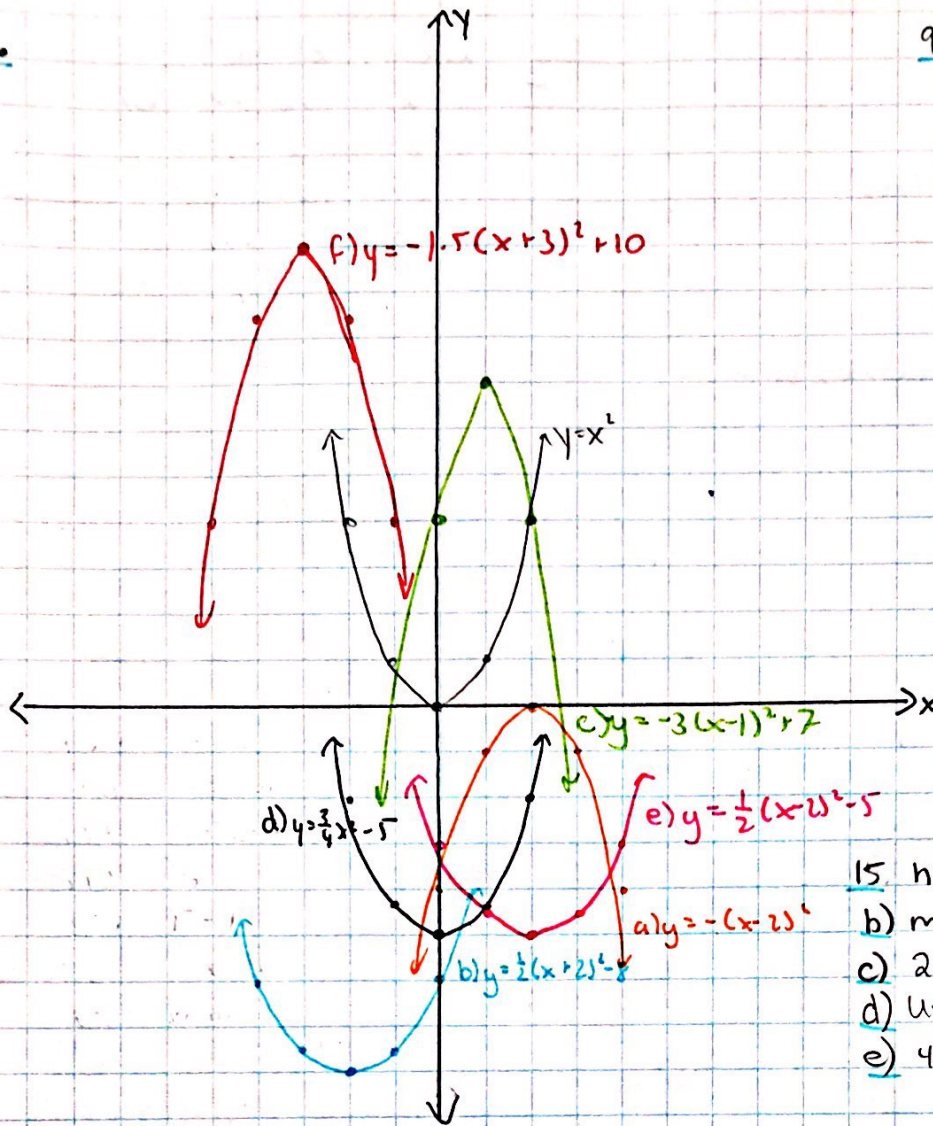


- ba) ii  
b) v  
c) iv  
d) vi  
e) i  
f) iii)

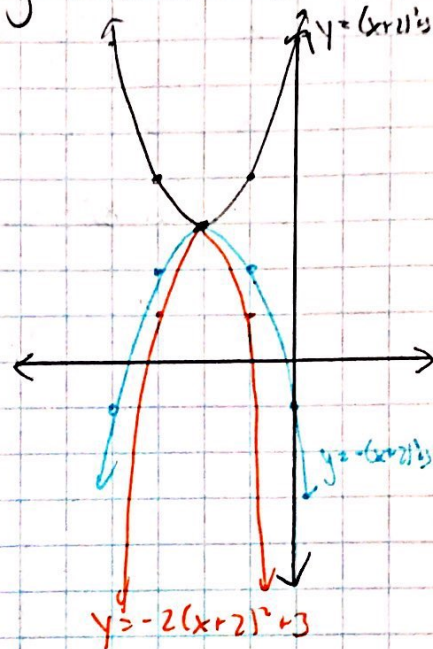
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	8.	Relation	Stretch/Comp Factor	Reflection?	Translation	Vertex	A of S
a)	iv	$y = 4(x+2)^2 - 3$	4	no	← 2, ↓ 3	$(-2, -3)$	$x = -2$
b)	vi	$y = -(x-1)^2 + 4$	1	yes	→ 1, ↑ 4	$(1, 4)$	$x = 1$
c)	iii)	$y = 0.8(x-6)^2$	0.8	no	→ 6	$(6, 0)$	$x = 6$
d)	v	$y = 2x^2 - 5$	2	no	↓ 5	$(0, -5)$	$x = 0$
Top	ii	$y = 3(x-2)^2 - 5$	3	no	→ 2, ↓ 5	$(2, -5)$	$x = 2$

7.



9.  $y = (x+2)^2 + 3$   
 $y = -(x+2)^2 + 3$  (reflection)  
 $y = -2(x+2)^2 + 3$  (stretch)  
 $y = (x+2)^2$



15.  $h = -5(t-2)^2 + 21$   
 b) max height is 21m  
 c) 2 seconds  
 d) Use your graph to estimate  
 e) 4.05 seconds.

10.  $h = -0.5(g-r)t^2 + t$

$g = 9.8$

$r_1 = 0.6$  (bedsheet)

$r_2 = 2.1$  (car tarp)

$r_3 = 8.9$  (parachute)

a) Bed sheet

$h = -0.5(9.2)t^2 + 100$

$h = -4.6t^2 + 100$

Car tarp

$h = -0.5(7.7)t^2 + 100$

$= -3.85t^2 + 100$

Parachute

$h = -0.5(0.9)t^2 + 100$

$= -0.45t^2 + 100$

b) yes, but the parachute would need to be much closer to the ground.

11a)  $y = -x^2 + 5$

b)  $y = 5(x+2)^2$

c)  $y = \frac{1}{5}x^2 - 6$

d)  $y = -6(x-3)^2 + 4$

12.

13.  $y = -\frac{2}{3}(x-3)^2 + 5$

Vertex: (3, 5)

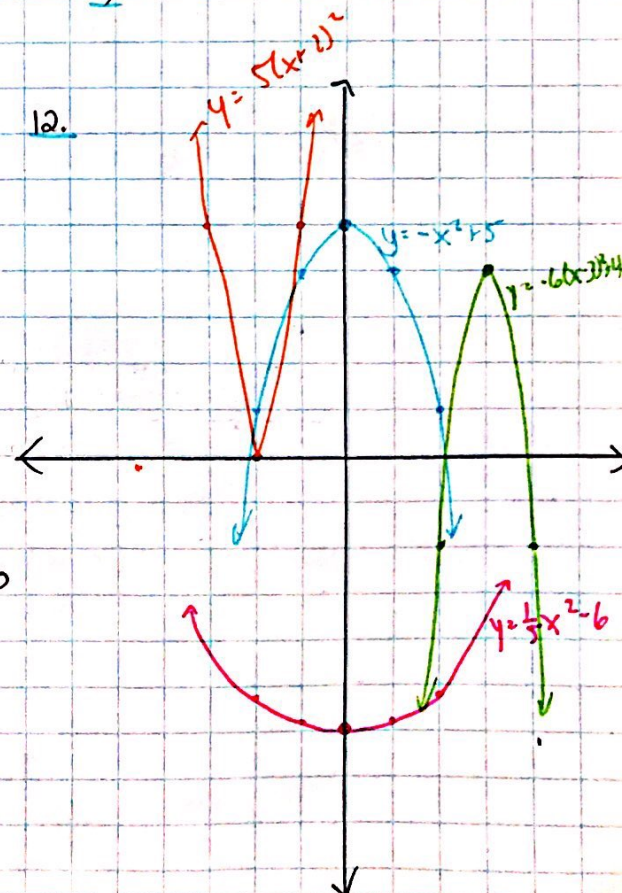
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14.  $h = -5(t-4)^2 + 2500$

a) 4 seconds

b) 2500m



$$17. y = 2(x-4)(x+10)$$

Vertex:

$$x = \frac{4-10}{2} \quad y = 2(-7)(7)$$

$$= -98$$

$$x = -3$$

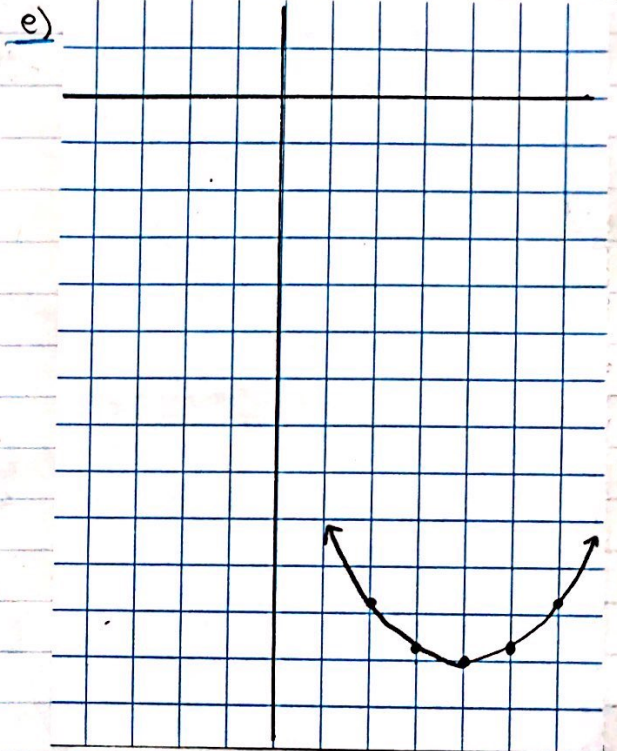
$$y = 2(x+3)^2 - 98 \quad (\text{vertex form})$$

$$\begin{aligned} y &= 2(x-4)(x+10) \\ &= 2(x^2 + 10x - 4x - 40) \\ &= 2(x^2 + 6x - 40) \\ &= 2x^2 + 12x - 80 \\ & \text{(standard form)} \end{aligned}$$

## 5.4 Quadratic Models Using Vertex Form

1a) iii      2a)  $y = a(x-4)^2 - 12$   
b) iv        b)  $15 = a(13-4)^2 - 12$   
c) i             $27 = 81a$   
d) ii             $\frac{1}{3} = a$   
c)  $y = \frac{1}{3}(x-4)^2 - 12$

d) v.s. by a factor of  $\frac{1}{3}$   
 • shift right 4 units & down 12 units



3a)  $y = \frac{1}{4}x^2$  (step pattern)  
b) vertex  $(-1, 0)$ , point  $(-2, 2)$   
 $2 = a(-2+1)^2 + 0$   
 $2 = a$   
 $y = 2(x+1)^2$

c) vertex  $(0, 4)$ , point  $(2, 0)$   
 $0 = a(2-0)^2 + 4$   
 $-4 = 4a$   
 $-1 = a$

$y = -x^2 + 4$

d) vertex  $(1, 2)$  point  $(-1, 2)$   
 $-2 = a(-1-1)^2 + 2$   
 $-4 = 4a$   
 $-1 = a$

$y = -(x-1)^2 + 2$

e) vertex  $(2, 4)$ , point  $(3, 1)$   
 $1 = a(3-2)^2 + 4$   
 $-3 = a$

$y = -3(x-2)^2 + 4$

f) vertex  $(-2, -3)$ , point  $(-3, 2)$   
 $2 = a(-3+2)^2 - 3$   
 $5 = a$

$y = 5(x+1)^2 - 2$

4a)  $y = 4x^2$

b)  $y = (x+3)^2$

c)  $y = -x^2 + 2$

d)  $y = \frac{1}{2}x^2$

e)  $y = (x-5)^2 - 4$

f)  $y = 2(x-1)^2$

5a)  $y = x^2 + 4$

b)  $y = -(x-5)^2$

c)  $y = -2(x-2)^2 - 3$

d)  $y = -\frac{1}{2}(x+3)^2 + 5$

e)  $y = 2(x-4)^2 - 3$

f)  $y = -\frac{1}{2}(x-3)^2 + 4$

*Milroy*

$$6a) 1 = a(-4+2)^2 + 3$$

$$-2 = 4a$$

$$-\frac{1}{2} = a$$

$$y = -\frac{1}{2}(x+2)^2 + 3$$

$$b) 1 = a(0+1)^2 - 1$$

$$2 = a$$

$$y = 2(x+1)^2 - 1$$

$$c) 6 = a(-5+2)^2 - 3$$

$$9 = 9a$$

$$1 = a$$

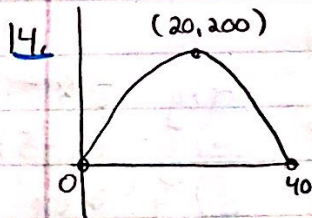
$$y = (x+2)^2 - 3$$

$$d) -4 = a(1+2)^2 + 5$$

$$-9 = 9a$$

$$-1 = a$$

$$y = -(x+2)^2 + 5$$



- find an equation in factored form
- find an equation in vertex form.

$$18. a=3, \text{ so}$$

$$y = 3(x+1)^2 + 4$$

$$y = 3(x^2 + 2x + 1) + 4$$

$$= 3x^2 + 6x + 7$$

$$\text{so } b=6, c=7$$

$$7a) x=5$$

$$y = -4(x-5)^2 + 3$$

$$b) x=6$$

$$8. \text{ vertex: } (3, 2), \text{ point } (6, 0)$$

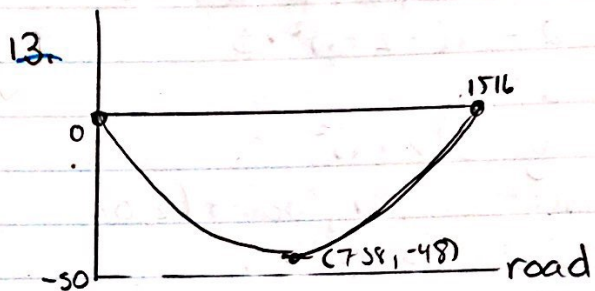
$$y = a(x-h)^2 + k$$

$$0 = a(6-3)^2 + 2$$

$$-2 = 9a$$

$$-\frac{2}{9} = a$$

$$y = -\frac{2}{9}(x-3)^2 + 2$$



$$0 = a(0-758)^2 - 48$$

$$48 = 574564a$$

$$\frac{48}{574564} = a$$

$$y = \frac{12}{143641}(x-758)^2 - 48$$

$$15. (75, 1600) \text{ vertex } (50, 1225) \text{ point}$$

$$1225 = a(50-75)^2 + 1600$$

$$-375 = 625a$$

$$-\frac{3}{5} = a$$

$$y = -\frac{3}{5}(x-75)^2 + 1600$$

$$17a) y = 2(x-1)^2 - 1$$

$$b) y = -2(x+3)^2 + 1$$

$$c) y = -2(x+3)^2 - 4$$

$$d) y = 12(x-1)^2 + 1$$

$$e) y = -\frac{1}{2}(x-1)^2 + 1$$

$$19. a(x-h)^2 + k = 0$$

$$a(x-h)^2 = -k$$

$$(x-h)^2 = -\frac{k}{a}$$

$$x-h = \pm\sqrt{-\frac{k}{a}}$$

$$x = \pm\sqrt{\frac{k}{a}} + h$$

## 5.5 Solving Problems Using Quadratic Relations

1a)  $y = 2x^2 + 3$

b)  $y = 3(x-2)^2$

c)  $y = -(x-3)^2 - 2$

d)  $y = 0.5(x+3.5)^2 + 18.3$

2a)  $y = 3$  (min)

b)  $y = 0$  (min)

c)  $y = 2$  (max)

d)  $y = 18.3$  (min)

3a)  $-1.5 = a(5)^2$

$-\frac{3}{50} = a$

$y = -\frac{3}{50}x^2$

b) The values of 'a' are equal.

4a)  $-5 = a(2-0)^2 + 3$

$-5 = 4a + 3$

$-8 = 4a$

$-2 = a$

$y = -2x^2 + 3$

b)  $9 = a(5-2)^2$

$9 = 9a$

$1 = a$

$y = (x-2)^2$

c)  $14 = a(-1+3)^2 + 2$

$12 = 4a$

$3 = a$

$y = 3(x+3)^2 + 2$

d)  $-8 = a(1-5)^2 - 3$

$-5 = 16a$

$-\frac{5}{16} = a$

$y = -\frac{5}{16}(x-5)^2 - 3$

5a)  $0 = a(1+1)^2 - 4$

$4 = 4a$

$1 = a$

$y = (x+1)^2 - 4$

b)  $6 = a(6-4)^2 - 2$

$8 = 4a$

$2 = a$

$y = 2(x-4)^2 - 2$

c)  $0 = a(6-4)^2 + 4$

$-4 = 4a$

$-1 = a$

$y = -(x-4)^2 + 4$

d)  $2 = a(0-2)^2 + 4$

$-2 = 4a$

$-\frac{1}{2} = a$

$y = -\frac{1}{2}(x-2)^2 + 4$

6a)  $y = (x+1)(x+1) - 4$

$= x^2 + 2x + 1 - 4$

$= x^2 + 2x - 3$

b)  $y = 2(x-4)(x-4) - 2$

$= 2(x^2 - 8x + 16) - 2$

$= 2x^2 - 16x + 30$

c)  $y = -(x-4)(x-4) + 4$

$= -(x^2 - 8x + 16) + 4$

$= -x^2 + 8x - 12$

d)  $y = -\frac{1}{2}(x-2)(x-2) + 4$

$= -\frac{1}{2}(x^2 - 4x + 4) + 4$

$= -\frac{1}{2}x^2 + 2x + 2$

7  $y = a(x-r)(x-s)$

$8 = a(0-8)(0+2)$

$8 = -16a$

$-\frac{1}{2} = a$

$y = -\frac{1}{2}(x-8)(x+2)$

$y = -\frac{1}{2}(3-8)(3+2)$

$= -\frac{1}{2}(-5)(5)$

$= \frac{25}{2}$

$\therefore y = -\frac{1}{2}(x-3)^2 + \frac{25}{2}$

8  $y = 2(x+4)^2 - 7$

$y = 2(x-1)^2 - 10$

minimum is  $y = -10$

9a)  $y = (x-4)(x-4) - 1$

$= x^2 - 8x + 15$

$= (x-5)(x-3)$

b)  $y = 2(x+1)(x+1) - 18$

$= 2(x^2 + 2x + 1) - 18$

$= 2x^2 + 4x - 16$

$y = 2(x^2 + 2x - 8)$

$= 2(x-2)(x+4)$

9c)  $y = -(x+5)(x+5) + 1$

$= -(x^2 + 10x + 25) + 1$

$= -x^2 - 10x - 24$

$y = -(x^2 + 10x + 24)$

$= -(x+6)(x+4)$

d)  $y = -3(x+3)(x+3) + 75$

$= -3(x^2 + 6x + 9) + 75$

$= -3x^2 - 18x + 48$

$y = -3(x^2 + 6x - 16)$

$= -3(x+8)(x-2)$

Vertex:

$x = \frac{-2+8}{2}$

$= 3$

$x = 3$

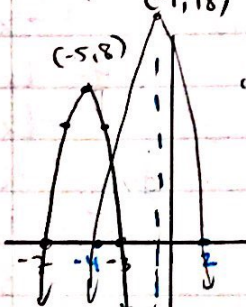
10a)  $y = 2x^2 - 12x$   
 $y = 2x(x-6)$   
 zeros:  $(0,0) + (6,0)$   
 vertex:  $x = 3$   
 $y = 2(3)^2 - 12(3)$   
 $= 18 - 36$   
 $= -18$

Vertex:  $(3, -18)$   
 $y = 2(x-3)^2 - 18$

d)  $y = (2x+5)^2$   
 zero:  $(-\frac{5}{2}, 0)$   
 Vertex is the zero  
 $y = 4(x + \frac{5}{2})^2$

12.  $y = -2(x+5)^2 + 8$   
 Zeros: Let  $y = 0$   
 $-8 = -2(x+5)^2$   
 $4 = (x+5)^2$   
 $\pm 2 = x+5$   
 $x = 2-5 \quad x = -2-5$   
 $= -3 \quad = -7$

Original zeros were  $(-3, 0)$  and  $(-7, 0)$



$\therefore$  The graph was moved 4 units right and 10 units up.

new  $a$  of  $x = -1$   
 $y = a(x-r)(x-s)$   
 $-2 = -2(-1+4)(-1-2)$   
 $-2 = -2(3)(-3)$   
 $\therefore \therefore$  New vertex:  $(-1, 18)$

b)  $y = -2x^2 + 24x - 64$   
 $= -2(x^2 - 12x + 32)$   
 $= -2(x-8)(x-4)$   
 vertex:  $x = 6$   
 $y = -2(6-8)(6-4)$   
 $= 8$   
 Vertex  $(6, 8)$   
 $y = -2(x-6)^2 + 8$

c)  $y = 2x^2 - x - 6$   
 $= (2x+3)(x-2)$   
 zeros:  $(-\frac{3}{2}, 0), (2, 0)$   
 vertex:  $x = \frac{1}{4}$   
 $y = 2(\frac{1}{4})^2 + 3(\frac{1}{4}-2)$   
 $= (\frac{7}{2})(-\frac{7}{4})$   
 $= -\frac{49}{8}$   
 $y = 2(x - \frac{1}{4})^2 - \frac{49}{8}$

11. Let  $x$  be the number of  $\$0.50$  price increases.  
 $y = (5 + 0.5x)(300 - 30x)$  zeros:  $-10 + 10$   
 Vertex:  $(0, 1500)$   
 $\therefore$  The current price of  $\$5$  maximizes the revenue.

13.  $C = 0.06t^2 - 0.27t + 5.36$

$x = \frac{-b}{2a}$   
 $= \frac{0.27}{0.12}$   
 $= \frac{9}{4}$

$C = 0.06(\frac{9}{4})^2 - 0.27(\frac{9}{4}) + 5.36$   
 $= \frac{3}{50}(\frac{81}{16}) - \frac{243}{400} + \frac{536}{100}$   
 $= \frac{243}{800} - \frac{243}{400} + \frac{2144}{400}$   
 $= \frac{243}{800} + \frac{1901}{400}$   
 $= \frac{4045}{800}$

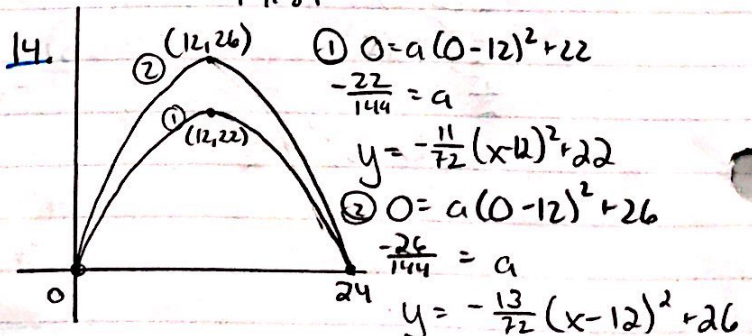
a) 1997

b)  $t = 3 \quad C = 0.06(3)^2 - 0.27(3) + 5.36$

c)  $t = 15 \quad = 85.09$

$C = 0.06(15)^2 - 0.27(15) + 5.36$   
 $=$

d)  $y = 0.06(x - \frac{9}{4})^2 + 5.05625$   
 $= 814.81$



①  $0 = a(0-12)^2 + 22$   
 $-\frac{22}{144} = a$

$y = -\frac{11}{72}(x-12)^2 + 22$

②  $0 = a(0-12)^2 + 26$   
 $-\frac{26}{144} = a$

$y = -\frac{13}{72}(x-12)^2 + 26$

15.  $P = 20(15-x)(11+x)$

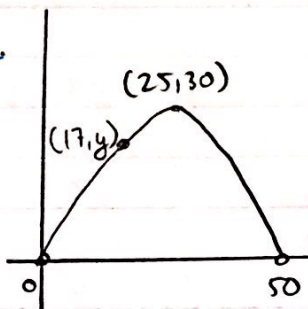
a)  $x = \frac{15-11}{2}$   
 $= 2$

$P = 20(15-2)(11+2)$   
 $= 20(13)(13)$   
 $= 338$

$P = 20(x-2)^2 + 338$

b) ∴ They maximize profit at \$13, and sell 338 tickets.

16.



$0 = a(0-25)^2 + 30$

$\frac{-30}{625} = a$

$-\frac{6}{125} = a$

$y = -\frac{6}{125}(x-25)^2 + 30$

Let  $x = 17$ :

$y = -\frac{6}{125}(17-25)^2 + 30$

$= -\frac{6}{125}(64) + 30$

$= -\frac{384}{125} + \frac{3750}{125}$

$= \frac{3366}{125}$

$= 26.9m$

∴ The sailboat will not fit!

17.  $y = ax^2 + bx + c$ ,  $c = -4$

①  $8 = a(-2)^2 + b(-2) - 4$     ②  $-1 = a(1)^2 + b(1) - 4$

$8 = 4a - 2b - 4$

$3 = a + b$

$2a - b = 6$

$12 = 4a - 2b$

Use elimination/substitution:  $\oplus \frac{a+b=3}{2a-b=6}$

①  $\div 2 \Rightarrow 6 = 2a - b$

$3a = 9$

$a = 3$

\* You can also draw it + use the step pattern!

∴  $y = 3x^2 - 4$   
 vertex  $(0, -4)$

$b = 0$

18. No! Vertex form  $\rightarrow$  vertex

Factored form  $\rightarrow$  zeros

Standard form  $\rightarrow$  y-intercept

*Hilary*

## 5.6 Connecting Standard and Vertex Form

1.  $x = \frac{2-6}{2}$   
 $x = -2$

2.  $y = 4x(x-3) + 5$  <sup>y-int</sup>  
 $x=0 \rightarrow (0, 5)$   $x=3 \rightarrow (3, 5)$

3.  $y = 2x^2 - 10x + 11$   
 $y = 2x(x-5) + 11$   
 $x=0 \rightarrow (0, 11)$   $x=5 \rightarrow (5, 11)$   
 $x = \frac{0+5}{2} = 2.5$   $y = 2(2.5)^2 - 10(2.5) + 11 = -3.5$

4a)  $x = \frac{3+7}{2}$   
 $x = 5$

5a)  $y = (x-1)(x+7)$   
 i)  $(1, 0)$  and  $(-7, 0)$   
 ii)  $x = \frac{1-7}{2} = -3$   $y = (-3-1)(-3+7) = -16$

$x = 2.5$  Vertex  $(\frac{5}{2}, -\frac{7}{2})$

b)  $-24 = a(9-3)(9-7)$   
 $-24 = a(6)(2)$   
 $-2 = a$   
 $y = -2(x-3)(x-7)$   
 When  $x=5$ ,  
 $y = -2(5-3)(5-7)$   
 $= -2(2)(-2)$   
 $= 8$

iii) Vertex  $(-3, -16)$   
 iv)  $y = (x+3)^2 - 16$   
 b)  $y = x(x-6) - 8$   
 i)  $x=0 \rightarrow (0, -8)$   $x=6 \rightarrow (6, -8)$   
 ii)  $x = 3$

5d)  $y = x(3x+12) + 2$   
 i)  $x=0 \rightarrow (0, 2)$   $x=-4 \rightarrow (-4, 2)$   
 ii)  $x = -2$   
 iii)  $y = -2(3(-2)+12) + 2$   
 $= -2(6) + 2$   
 $= -10$   
 $(-2, -10)$

Vertex:  $(5, 8)$

iii)  $y = 3(3-6) - 8$   
 $= 3(-3) - 8$   
 $= -17$   
 $(3, -17)$

iv)  $y = 3(x+2)^2 - 10$

6.  $y = -(x-4)^2 + 2$

7a)  $y = x^2 - 6x + 5$   
 $y = x(x-6) + 5$   
 $x=0, x=6$   
 $x=3$

iv)  $y = (x-3)^2 - 17$   
 c)  $y = -2(x+3)(x-7)$   
 i)  $(-3, 0), (7, 0)$   
 ii)  $x = \frac{-3+7}{2} = 2$

e)  $y = x^2 + 5x$   
 i)  $y = x(x+5)$   
 $x=0 \rightarrow (0, 0)$   $x=-5 \rightarrow (-5, 0)$   
 ii)  $x = -2.5$   
 iii)  $y = (-\frac{5}{2})^2 + 5(-\frac{5}{2})$   
 $= \frac{25}{4} - \frac{25}{2}$   
 $= -\frac{25}{4}$   
 $(-\frac{5}{2}, -\frac{25}{4})$

$y = (3)^2 - 6(3) + 5$   
 $= 9 - 18 + 5$   
 $= -4$

iii)  $y = -2(2+3)(2-7)$   
 $= -2(5)(-5)$   
 $= 50$

iv)  $y = (x + \frac{5}{2})^2 - \frac{25}{4}$

$(3, -4)$

$(2, 50)$

7c)  $y = -2x(x-6) - 11$   
 $x=0 \rightarrow (0, -11)$   $x=6 \rightarrow (6, -11)$

$y = (x-3)^2 - 4$

iv)  $y = -2(x-2)^2 + 50$

$x=3$

$y = -2(3)^2 + 12(3) - 11$   
 $= -18 + 36 - 11$   
 $= 7$

b)  $y = x(x-4) - 11$   
 $x=0 \rightarrow (0, -11)$   $x=4 \rightarrow (4, -11)$   
 $x=2$   
 $y = (2)^2 - 4(2) - 11$   
 $= -15$

$y = (x-2)^2 - 15$

$y = -2(x-3)^2 + 7$

7d)  $y = -x(x+6) - 13$   
 $x=0$        $x=-6$   
 $x = -3$   
 $y = (-3)^2 - 6(-3) - 13$   
 $= -9 + 18 - 13$   
 $= -4$

$(-3, -4)$

$y = -(x+3)^2 - 4$

e)  $y = -\frac{1}{2}x(x-4) - 3$   
 $x=0$        $x=4$

$x = 2$

$y = -\frac{1}{2}(2)^2 + 4(2) - 3$   
 $= -2 + 8 - 3$   
 $= 3$

$(2, 3)$

$y = -\frac{1}{2}(x-2)^2 + 3$

f)  $y = 2x(x-5) + 11$   
 $x=0$        $x=5$

$x = \frac{5}{2}$

$y = 2(\frac{5}{2})^2 - 10(\frac{5}{2}) + 11$   
 $= 2(\frac{25}{4}) - 25 + 11$   
 $= \frac{25}{2} - 14$   
 $= -\frac{3}{2}$

$(\frac{5}{2}, -\frac{3}{2})$

$y = 2(x - \frac{5}{2})^2 - \frac{3}{2}$

12.  $h = -5t^2 + 9t + 1$

$t = \frac{-9}{-10}$

$= \frac{9}{10}$

$h = -5(\frac{9}{10})^2 + 9(\frac{9}{10}) + 1$

$= -\frac{81}{20} + \frac{81}{10} + 1$

$= 5\frac{1}{20}$  The max ht is 5.05m.

8. ① Factor

$y = -2(x^2 - 8x + 12)$   
 $= -2(x-6)(x-2)$

zeros:  $(6, 0), (2, 0)$

a of 5:  $x = 4$

②  $x = \frac{-b}{2a}$   
 $x = \frac{-16}{2(-2)}$   
 $= \frac{-16}{-4}$

$x = 4$

Option 2 is faster!

9.  $y = ax^2 + bx + 7$  ← point  $(0, 7)$   
 $y = a(x-4)^2 + 5$

$7 = a(0-4)^2 + 5$

$12 = 16a$

$\frac{3}{4} = a$

$y = \frac{3}{4}(x-4)^2 + 5$   
 $= \frac{3}{4}(x^2 - 8x + 16) + 5$   
 $= \frac{3}{4}x^2 - 6x + 7$

10.  $8 = a(0-1)^2 + 7$

$1 = a$

$y = (x-1)^2 + 7$   
 $= x^2 - 2x + 8$

11.  $h = -5t^2 + 150t$

$t = \frac{-b}{2a}$

$= \frac{-150}{-10}$

$= 15s$

$h = -5(15)^2 + 150(15)$   
 $= 1125m$

∴ The max height is 1125m

13.  $P = -30t^2 + 450t - 790$

$t = \frac{-450}{-60}$

$= \frac{15}{2}$

∴ \$7.50 will maximize profit.

$$14. G = 1492 - 76t + 5.2t^2$$

$$a) t = \frac{76}{2(5.2)}$$

$$= 7.3$$

∴ The minimum production occurred in 1977.

$$b) G = 1492 - 76(7.31) + 5.2(7.31)^2$$

$$= 1214.1 \text{ tonnes}$$

$$c) t = 15$$

$$G = 1492 - 76(15) + 5.2(15)^2$$

$$= 1522 \text{ tonnes}$$

17. Let  $x$  be the number of \$0.05 price increases.

$$R = (1.75 + 0.05x)(9450 - 210x)$$

$$\text{Zeros: } 0.05x = -1.75 \quad 210x = 9450$$

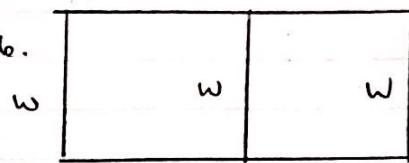
$$x = -35 \quad x = 45$$

$$x = \frac{45 - 35}{2}$$

$$= 5 \leftarrow \text{price increases } (\$0.25)$$

The need to charge \$2.00, and they will lose 1050 customers.

16.



He can buy  $3000 \div 5 = 600$  m of fencing

$$2l + 3w = 600 \rightarrow \textcircled{1} l = -\frac{3}{2}w + 300$$

$$\textcircled{2} A = lw$$

$$A = -\frac{3}{2}w^2 + 300w$$

$$w = \frac{-300}{-3} \quad l = 150$$

$$= 100$$

$$A = -\frac{3}{2}(100)^2 + 300(100)$$

$$= 15000 \text{ m}^2$$