

Wednesday, October 10, 2018

8.1 Vector and Parametric Equations of a Line in \mathbb{R}^2

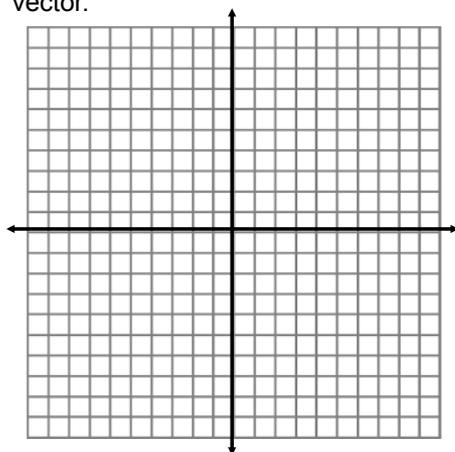
What forms of an equation of a line do we already know?



Any point on the line will satisfy all of those equations. These forms only work in two dimensions though. In order to extend equations into three space, we need to look at new forms of the equation of a line.

1) Vector Equation of a Line in a Plane

If we have a line with a slope of $3/2$ that passes through $A(-1, 4)$, we can also describe it as a line that moves in the same direction as the direction vector $\vec{d} = (2, 3)$. Any scalar multiple of d is also a direction vector.



In general, the vector equation of a line in a plane is:

$$\vec{r} = (x_0, y_0) + t(a, b)$$

where $\vec{r} = (x, y)$ is the position vector of any point on the line, (x_0, y_0) is the position vector of a particular point on the line, and (a, b) is the direction vector, and $t \in \mathbb{R}$.

Example: Determine the vector equation of a line with a slope of 3 that passes through the point $(2, -5)$.

Note: If you are asked to identify if lines are coincident, you are just checking to see if their direction vectors are parallel.

